

Computer Graphics - Exercise 1

1.1.1

a)

- Matrix Multiplication \equiv transformation
- Inverse of a transformation \tilde{T}^{-1}

$$\begin{aligned} \Rightarrow \quad & \tilde{T} * \tilde{T}^{-1} = \tilde{T}^{-1} * \tilde{T} = \tilde{E} & \left| \begin{array}{l} * \tilde{p} \\ \tilde{T} * \tilde{p} = \tilde{p}' \end{array} \right. \\ & \tilde{T}^{-1} * \tilde{T} * \tilde{p} = \tilde{E} * \tilde{p} \\ \Rightarrow \quad & \tilde{E} * \tilde{p} = \tilde{p}, \quad \tilde{T}^{-1} * \tilde{p}' = \tilde{p} \end{aligned}$$

b)

1.1.2

a)

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} * \begin{pmatrix} x_1 & x_2 & \cdots & x_n \\ y_1 & y_2 & \cdots & y_n \\ z_1 & z_2 & \cdots & z_n \end{pmatrix} = \begin{pmatrix} x_1 & x_2 & \cdots & x_n \\ z_1 & z_2 & \cdots & z_n \\ y_1 & y_2 & \cdots & y_n \end{pmatrix}$$

b)

$$\begin{pmatrix} x_1 & x_2 & \cdots & x_n \\ y_1 & y_2 & \cdots & y_n \\ z_1 & z_2 & \cdots & z_n \end{pmatrix} * \begin{pmatrix} 1 \\ 1 \\ \vdots \\ 1 \end{pmatrix} = \begin{pmatrix} \sum_{i=1} x_i \\ \sum_{i=1} y_i \\ \sum_{i=1} z_i \end{pmatrix}$$

c)

$$\begin{aligned} L(p) &= length(p_x - ((p_x \cdot (\vec{e} + \vec{d} * t)) * \vec{d} * t) - \vec{e}) \\ Vector &= (L(p_x), L(p_{x+1}), \dots, L(p_{x+n})) \quad n \equiv Anz.Punkte \end{aligned}$$

Berechnung: